Question 1

If f is a differentiable function, find an expression for the derivative of each of the following functions.

(a)
$$y = x^2 f(x)$$

(b) $y = \frac{f(x)}{x^2}$
(c) $y = \frac{x^2}{f(x)}$
(d) $y = \frac{1 + xf(x)}{\sqrt{x}}$

Question 2

On what interval is the function $f(x) = x^2 e^x$ concave downward?

Question 3

Find the derivative of the following function.

$$y = e^{-7x} \cos 3x$$

Question 4

Find the derivative of the following function.

 $y = \tan^2 6x$

Question 5

Find $\frac{dy}{dx}$ by implicit differentiation.

$$y^5 + x^2 y^3 = 1 + y e^{x^2}$$

Differentiate the following function.

$$h(x) = \ln\left(x + \sqrt{x^2 - 1}\right)$$

Question 7

Find the linearization L(x) of the following function at a = -8.

$$f(x) = \sqrt[3]{x}$$

Question 8

Evaluate the following indefinite integral.

$$\int x^3 \left(1-x^4\right)^9 \, dx$$

Question 9

Evaluate the following integral using integration by parts with $y = \theta$ and $dv = \cos \theta \ d\theta$.

$$\int \theta \cos \theta \, d\theta$$

Question 10

Write out the form of the partial fraction expansion in each function. Do not determine the numerical values of the coefficients.

(a)
$$\frac{x-1}{x^3+x^2}$$

(b) $\frac{x-1}{x^3+x}$